

21. Correct. The answer is false. The profit functions for the two firms given the other firms output are:

$$\pi_1 = (200 - 0.7(q_1 + q_2))q_1 - 1.5q_1^2,$$

$$\pi_2 = (200 - 0.7(q_1 + q_2))q_2 - 1.8q_2^2.$$

First order conditions for profit maximization for the firms are:

$$\frac{\partial \pi_1}{\partial q_1} = 200 - 0.7(q_1 + q_2) - 0.7q_1 - 3q_1 = 0.$$

$$\frac{\partial \pi_2}{\partial q_2} = 200 - 0.7(q_1 + q_2) - 0.7q_2 - 3.6q_2 = 0$$

These equations can be rearranged into reaction functions as

$$q_1 = (200 - 0.7q_2)/4.4 = 45.455 - 0.159q_2$$

$$q_2 = (200 - 0.7q_1)/5 = 40.0 - 0.14q_1.$$

In the Stackleberg model, the firms do not collude, but the dominant firm, often called the price leader, optimizes given the other firm's reaction function.

Thus using the above equations:

$$\begin{aligned} \pi_1 &= (200 - 0.7(q_1 + q_2))q_1 - 1.5q_1^2 = 200q_1 - 0.7q_1^2 - 0.7q_2q_1 - 1.5q_1^2 \\ &= 200q_1 - 2.2q_1^2 - 0.7q_2q_1 \end{aligned}$$

Now substitute 2's reaction function into π_1

$$= 200q_1 - 2.2q_1^2 - 0.7(40.0 - 0.14q_1)q_1 = 172q_1 - 2.102q_1^2$$

First order conditions for 1 are:

$$\frac{\partial \pi_1}{\partial q_1} = 172 - 2*2.102q_1 = 172 - 4.204$$

$$q_1 = 0$$

$$q_1 = 172/4.204 = \mathbf{40.913}$$

q_2 's reaction function is the same as before

$$q_2 = 28.0 - 0.14q_1 = 40.0 - 0.14(40.913) = \mathbf{34.272}$$

Finally, the price can be calculated from the inverse demand equation as follows,

$$P = 200 - 0.7(q_1 + q_2) = 200 - 0.7(40.913 + 34.272) = \mathbf{147.37}$$